

# AUTOMATED TENSION CONTROL SYSTEM OF TRACK BELT FOR BULLDOZING OPERATION

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## SUMMARY

As the flexibility of track belt running on a weak terrain affects the shape of contact pressure distribution, the flexibility is dominant not only over the thrust developed under the track belt but over the amount of slip sinkage at the rear sprocket. Here, the relations between track tension, normal and shear stress distribution, and the amount of static and slip sinkages have been presented for a flexible tracked bulldozer running on a weak silty loam terrain by means of the rigorous simulation programme. As the results, it is clarified that the effective tractive effort increases monotonously and the amount of total sinkage of rear sprocket decreases remarkably with the increment of track tension. For adjusting the track tension to the optimum flexibility corresponding to the running terrain, an automated tension control system of the track belt should be established by use of some track tension sensor or rut depth sensor.

*Key words : track tension, flexible tracked vehicle, effective tractive effort, weak terrain, sinkage*

## 1. Introduction

The productivity of bulldozer having a flexible track belt running on a weak terrain is considered to vary remarkably with the flexibility of the track belt. It is necessary to control the track belt tension in moderate state at all times, because the tension used to drop down gradually due to the abrasive wear of tread parts of frontidler, pin and bush of link etc.. As there is an optimum flexibility of track belt for a given terrain to maximize the optimum effective tractive effort, the flexibility should be considered as one of the most important factors to obtain the maximum productivity or the maximum efficiency of bulldozer. The shape of distribution of contact pressure depends considerably on the flexibility, so the track tension gives an important effect on the thrust developed under the track belt and the rut depth of bulldozer. Here, several relations between the track tension, the effective tractive effort, and the amount of sinkage of rear sprocket have been analysed for a given bulldozer running on the weak ground of given terrain-track system constants by means of the new developed simulation programme. Afterwards, several methods to set the control system of the flexibility of track belt are considered by use of some tension sensor or rut depth sensor.

## 2. Flexibility and track tension

Fig.1 shows the several forces acting on the flexible track belt.



The following condition of equilibrium may be written if the denotations in the figure are followed :

$$\begin{aligned} F &= T_0 \tan \delta \\ &= T_0 \frac{d S_{oi}'(X)}{d X} \end{aligned} \quad (1)$$

where  $F$  is the ground reaction between the central point  $O_m$  of the adjacent two track rollers and the arbitrary point  $A$ ,  $T_0$  is the tension force acting upon the point  $O_m$ , and  $S_{oi}'(X)$  is the amount of static sinkage of track belt at the distance  $X$  from the contact point of frontidler on the main part of track belt<sup>1)</sup>,

The ground reaction  $F = F(X)$  could be calculated approximately as the integration of normal contact pressure  $p_{oi}(X)$  of rigid track belt from the point  $O_m : X = (20m-10)d$  to the point  $A : X = nd$  where  $m$ ,  $n$  is a positive integer and  $d = D/N$  is the minute interval of the contact length of track belt  $D$ . That is,

$$F(X) = B \int_{(20m-10)d}^{nd} p_{oi}(X) dx \quad (2)$$

$$(20m-20 < n < 20m)$$

where  $B$  is the track width.

And  $T_0$  is the summation of the initial track tension force  $H_0$  and the thrust  $H_m$  acting upon the interface of track belt and ground.  $H_m$  could be calculated as the integration of shear resistance  $\tau(X)$  of ground from the contact point of frontidler on the main part of track belt :  $X=0$  to the point  $O_m : X = (20m-10)d$ . That is,

$$H_m = B \int_0^{(20m-10)d} \tau(X) dX \quad (3)$$

Therefore, the distribution of static sinkage of the flexible track belt could be calculated from Eqs.(1)(2) and (3) as,

$$\begin{aligned} S_{oi}'(X) &= \frac{1}{H_0 + H_m} \int_{(20m-10)d}^{nd} F(X) dX + C \\ C &= S_{oi}\{(20m-10)d\} \end{aligned} \quad (4)$$

where  $C$  is the static sinkage of rigid track belt at  $X = (20m-10)d$ .

Then, the distribution of normal contact pressure  $p_{oi}'(X)$  of the flexible track belt could be calculated as

$$p_{oi}'(X) = k \{S_{oi}'(X)\}^n \quad (5)$$

On the other hand, the total sinkage of frontidler  $S_{fi}'$  could be calculated as

$$S_{fi}' = \{S_{oi}'(0) + S_{fs}'\} \cos \theta_{ti}' \quad (6)$$

$S_{fs}'$  is the slip sinkage<sup>2)</sup> given as

$$\begin{aligned} S_{fs}' &= c_0 \sum_{m=1}^M \{p_{roi}'(\theta_m)\}^{c_1} [(j_m)^{c_2} - (j_{m-1})^{c_2}] \cos \theta_m \\ p_{roi}'(\theta_m) &= k \{S(\theta_m)\}^n \end{aligned}$$

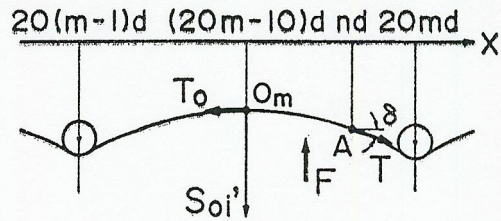


Fig.1 Several forces acting on flexible track belt



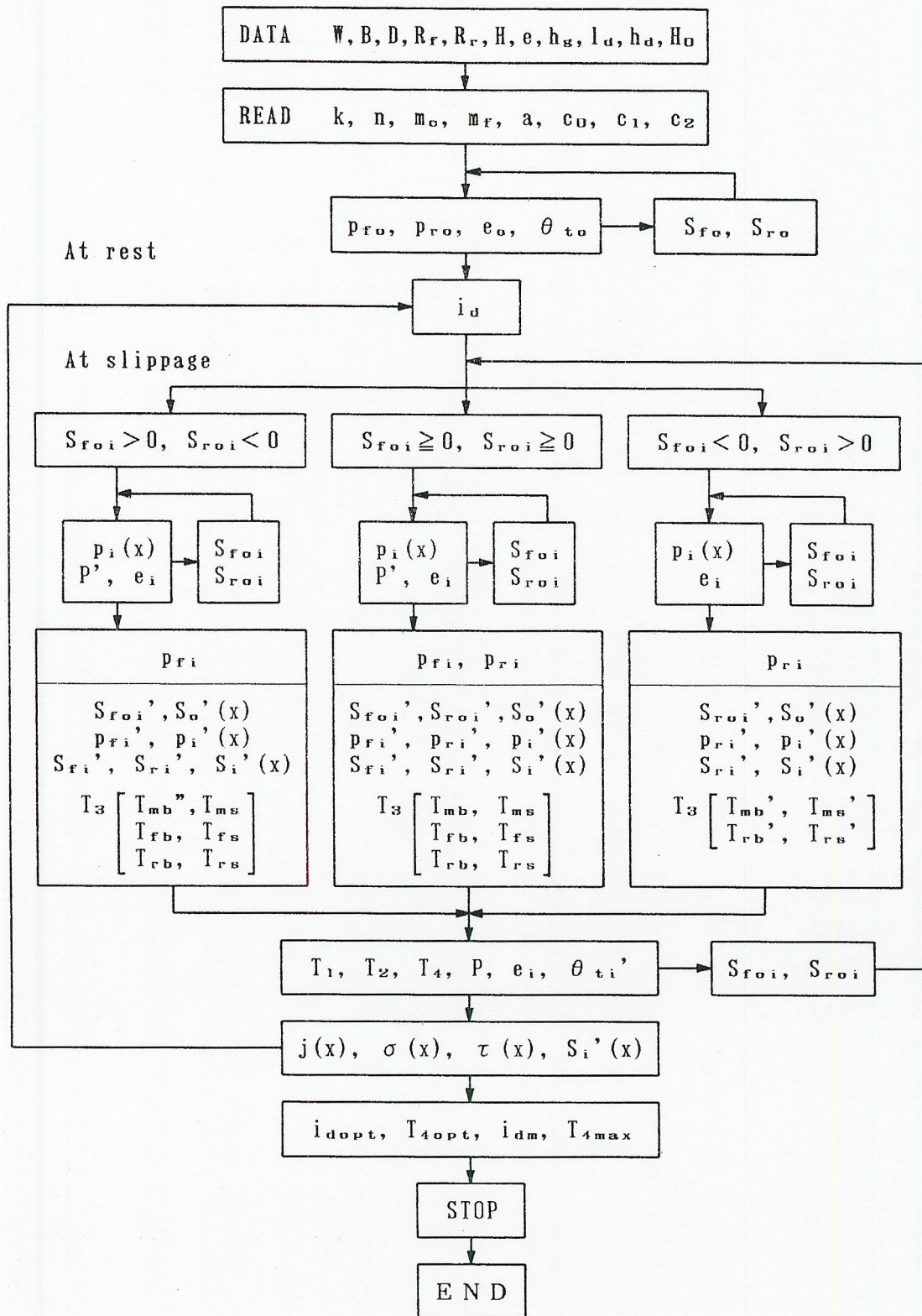


Fig.2 Flow chart



$$\begin{aligned}
S(\theta_m) &= \frac{R_f \{ \cos(\theta_m + \theta_{ti}) - \cos(\theta_r + \theta_{ti}) \}}{\cos(\theta_m + \theta_{ti})} \\
\theta_m &= \theta_r (1 - m/M) \\
\theta_r &= \cos^{-1} \left( \cos \theta_{ti}' - \frac{S_{ri}'}{R_f} \right) - \theta_{ti}' \\
\theta_{ti}' &= \sin^{-1} \left( \frac{S_{ri}' - S_{fi}'}{D} \right) \\
j_m &= \frac{R_f}{1 - i_d} \int_{\theta_m}^{\theta_r} \{ 1 - (1 - i_d) \cos \theta \} \cos \theta \, d\theta
\end{aligned}$$

where  $c_0$ ,  $c_1$  and  $c_2$  are constants,  $R_f$  is the radius of frontidler,  $i_d$  is slip ratio at driving state and  $\theta_{ti}'$  is the trim angle of vehicle.

The total sinkage of rear sprocket  $S_{ri}'$  could be calculated as

$$S_{ri}' = \{S_{oi}'(D) + S_{rs}'\} \cos \theta_{ti}' \quad (7)$$

$S_{rs}'$  is the slip sinkage given as

$$\begin{aligned}
S_{rs}' &= S_{rs}' + c_0 \sum_{n=1}^N \{p_{oi}'(n d)\}^{c_1} [(n q)^{c_2} - \{(n-1)q\}^{c_2}] \\
p_{oi}'(n d) &= \frac{1}{k} \{S_{oi}'(n d)\}^n \\
q &= i_d' D / \{(1 - i_d')N\}
\end{aligned}$$

The contact points among frontidler, each track roller, rear sprocket and main part of flexible track belt should be located on the next straight line.

$$S_i'(X) = S_{ri}' + (S_{ri}' - S_{fi}') \frac{X}{D} \quad (8)$$

Therefore, the final sinkage of flexible track belt  $S_i'(n d)$  at  $X = n d$  could be calculated for 7 intervals of track roller as

$$\begin{aligned}
S_i'(n d) &= S_{oi}'(n d) + S_i' \{ (20m-20)d \} - S_{oi}' \{ (20m-20)d \} \\
&\quad + \{ [S_i'(20m d) - S_{oi}'(20m d)] - [S_i' \{ (20m-20)d \} - S_{oi}' \{ (20m-20)d \}] \} \cdot \{ n d - (m-1) \frac{D}{8} \} / \frac{D}{8} \\
d &= D/N, \quad 20m-20 < n < 20m \\
m &= 1, 2, \dots, 8 \\
n &= 1, 2, \dots, N \quad (160)
\end{aligned} \quad (9)$$

### 3. Simulation programme

Table 1 shows the terrain-track system constants<sup>3)</sup> measured for the track model having 5 trapezoidal grousers of 6cm height, 18cm pitch, 2cm contact length and 9cm base which runs on the remolded silty loam terrain of 30% water content and 31kPa Cone Index. Table 2 shows the vehicle dimensions of a given bulldozer having the flexible track belt of the same trapezoidal grousers.

Fig.2 shows the flow chart to calculate the traffic performance of the flexible tracked vehicle running on the weak terrain. First of all, the initial data:  $W$ ,  $B$ ,  $D$ ,  $R_f$ ,  $R_r$ ,  $H$ ,  $e$ ,  $h_g$ ,  $l_d$ ,  $h_d$  and  $H_0$  are given. And the terrain-track system constants  $k$ ,  $n$ ,  $m_0$ ,  $m_f$ ,  $a$ ,  $c_0$ ,  $c_1$  and  $c_2$  are read as input data. At rest, the eccentricity  $e_0$  of resultant normal force  $P$  acting upon the track belt, the contact pressure  $p_{ro}$ ,  $p_{ro}$  at frontidler and rear sprocket, the trim angle of vehicle  $\theta_{to}$



Table 1 Vehicle dimensions

Vehicle Weight	$W$	117.6 kN
Width of track belt	$B$	150 cm
Contact length of track belt	$D$	280 cm
Mean contact pressure	$p_m$	13.7 kPa
Radius of frontidler	$R_f$	35 cm
Radius of rear sprocket	$R_r$	35 cm
Height of grouser	$H$	6 cm
Grouser pitch	$G_p$	18 cm
Interval of track roller	$R_p$	35 cm
Eccentricity of gravity center of vehicle	$e$	-0.02
Height of gravity center of vehicle	$h_g$	70 cm
Distance between central axis of vehicle and point acting effective tractive effort	$l_d$	290 cm
Height of point acting effective tractive effort	$h_d$	42 cm

Table 2 Terrain-track system constants

Static pressure sinkage test $k = 6.669$ $n = 0.594$
Shear deformation test $m_c = 3.626$ kPa $m_r = 0.356$ $a = 0.148$ 1/cm
Slip sinkage test $c_0 = 0.253$ $c_1 = 0.751$ $c_2 = 0.360$



are repeatedly calculated until the static sinkage  $S_{fo}$ ,  $S_{ro}$  at frontidler and rear sprocket are determined. At slippage state for a given  $i_d$ , the contact pressure  $p_{fi}$ ,  $p_{ri}$  and the distribution  $p_i(X)$  for an assumed rigid track belt, the modified resultant normal force  $P'$  for the force acting upon the frontidler, and the eccentricity  $e_i$  are repeated calculated until the static sinkages  $S_{foi}$  and  $S_{roi}$  are determined. Afterwards, the distributions of static sinkage  $S_o'(X)$ ,  $S_{foi}'$  and  $S_{roi}'$ , and contact pressure  $p_i'(X)$ ,  $p_{fi}'$  and  $p_{ri}'$  for the flexible track belt are obtained, and then the distribution of total sinkage  $S_i'(X)$  is determined as the summation of  $S_o'(X)$  and the slip sinkage calculated from  $p_i'(X)$ . The thrust  $T_3$  is calculated as the summation of shear resistance which develops on the interface between main part of bottom track belt  $T_{mb}$ ,  $T_{ms}$ , contact part of frontidler  $T_{fb}$ ,  $T_{fs}$  and that of rear sprocket  $T_{rb}$ ,  $T_{rs}$ , and the terrain <sup>2)</sup>. Then, the driving force  $T_1$ , the locomotion resistance  $T_2$ , the effective tractive effort  $T_4$ , the resultant normal force  $P$ , the eccentricity  $e_i$  and the trim angle  $\theta_{ti}'$  are repeatedly calculated until the static sinkages of the track belt  $S_{foi}$ ,  $S_{roi}$  are determined. There are 3 kinds of process which is divided by the sign of static sinkage of the flexible track belt. Finally, the relations between  $T_1, T_4 - i_d$ ,  $S_{fi}', S_{ri}' - i_d$ ,  $\theta_{ti}' - i_d$  and  $e_i - i_d$  are determined, and the distributions of amount of slippage  $j(X)$ , normal stress  $\sigma(X)$ , shear stress  $\tau(X)$  and total sinkage of track belt  $S_i'(X)$  are graphically shown by use of micro-computer.

#### 4. Analytical results

##### 4.1 Tractive performance

As an example, the tractive performance of the flexible tracked vehicle as shown in Table 2 has been simulated for the initial track tension force  $H_o = 9.8\text{kN}$ . Fig.3 shows the relations between  $T_1$ ,  $T_4$  and  $i_d$  at driving state.  $T_1$  decreases gradually with  $i_d$  from the maximum value  $102.0\text{kN}$  at  $i_d = 10\%$  and  $T_4$  decreases rapidly with  $i_d$  from the maximum one  $78.4\text{kN}$  at  $i_{dm} = 2\%$  due to the increasing locomotion resistance. Fig.4 shows the relations between  $S_{fi}'$ ,  $S_{ri}'$  and  $i_d$  at driving state.  $S_{ri}'$  is always larger than  $S_{fi}'$  due to the increasing slip sinkage with slip ratio. Fig.5 shows the relations between  $e_i$ ,  $\theta_{ti}'$  and  $i_d$ .  $e_i$  decreases gradually until the minimum value  $-0.0694$  at  $i_d = 86\%$  and then in-

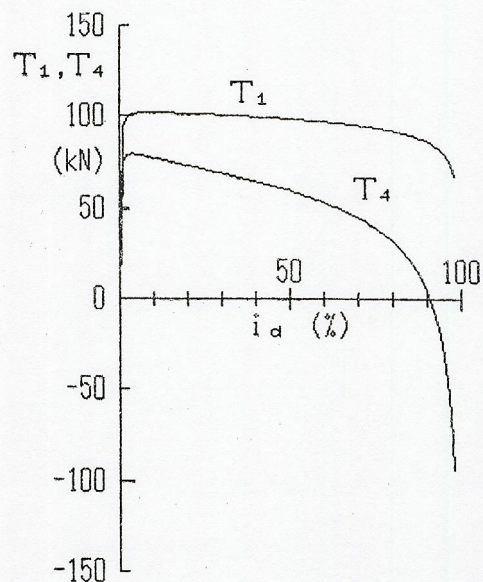


Fig.3 Driving force  $T_1$ , effective tractive effort  $T_4$  and slip ratio  $i_d$

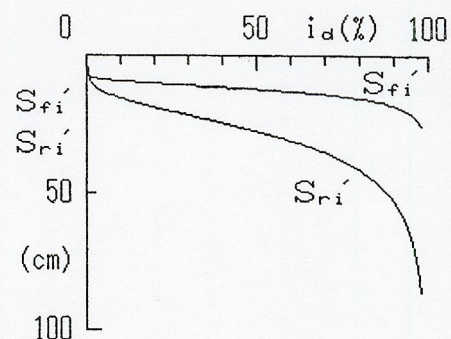


Fig.4 Total sinkages of frontidler and rear sprocket  $S_{fi}'$ ,  $S_{ri}'$  and slip ratio  $i_d$



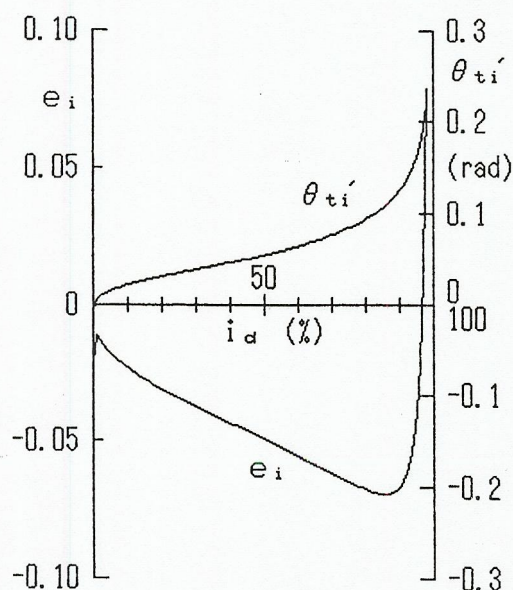


Fig.5 Eccentricity  $e_i$ , trim angle  $\theta_{ti}'$  and slip ratio  $i_d$

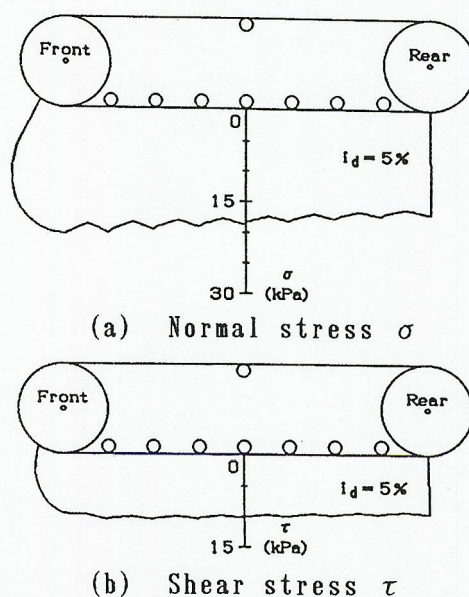


Fig.6 Distribution of contact pressure at driving state

creases rapidly at higher value of slip ratio.  $\theta_{ti}'$  increases parabolically with the increasing slip sinkage. Fig.6 shows the distributions of normal stress  $\sigma$  and shear stress  $\tau$  under the bottom track belt for  $i_d = 5\%$ . It shows some sinusoidal distribution, of which amplitude at front part of track belt is comparatively larger than that at the rear part due to the increasing thrust  $H_m$ . The amplitude of deflection of the track belt varies from 0.01cm to 0.52cm.

#### 4.2 Tension control system

The relations between tractive performance and track tension are simulated for the flexible tracked vehicle. Fig.7 shows the relations between the optimum effective tractive effort  $T_{4opt}$  at the optimum slip ratio  $i_{opt}$ <sup>3)</sup> and the track tension  $H_0$  for 3 kinds of eccentricity of the gravity center of the bulldozer.  $T_{4opt}$  increases gradually with the increment of  $H_0$ . Fig.8 shows the relations between the total sinkage of rear sprocket  $S_{ri}'$  and  $H_0$  in these cases, respectively.  $S_{ri}'$  decreases remarkably at the lower tension with the increment of  $H_0$ . Fig.9 shows that the traffic efficiency of power  $E_t$ <sup>4)</sup> at  $i_{opt}$  increases also at the lower tension with the increment of  $H_0$ . So, the track tension  $H_0$  should be controlled to set at some value as large as possible in these cases, by means of the hydraulic cylinder which is adjusted by some tension sensor or rut depth sensor.

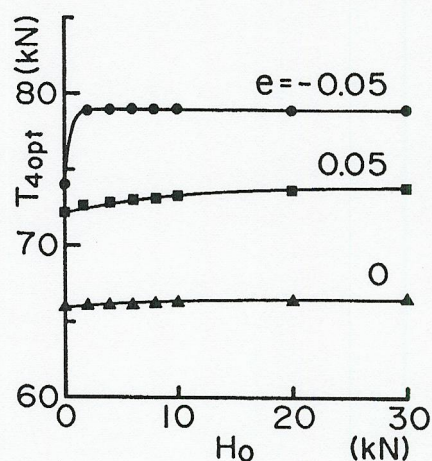


Fig.7 Optimum effective tractive effort  $T_{4opt}$  and initial track tension  $H_0$



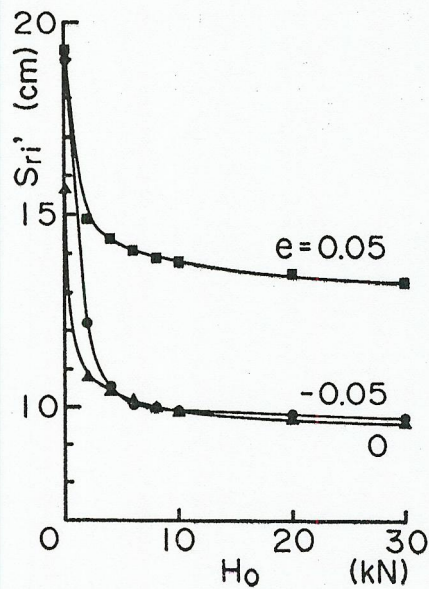


Fig.8 Total sinkage of rear sprocket  $S_{ri}'$  and initial track tension  $H_0$ .

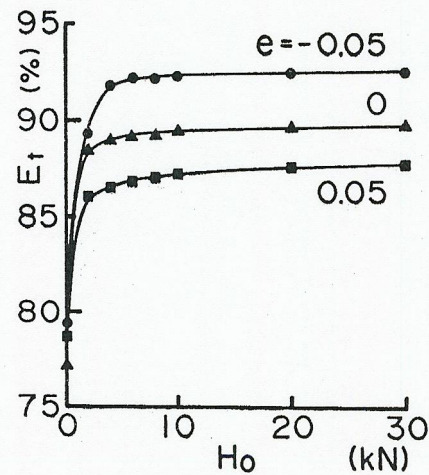


Fig.9 Traffic efficiency of power  $E_t$  and initial track tension  $H_0$ .

## 5. Conclusion

To establish an optimum operation of a flexible tracked vehicle running on a weak terrain, some tension control system of the track belt should be considered to improve the tractive performance. Here, the rigorous simulation programme has been developed to analyse the traffic performance of a bulldozer, considering the flexibility of the track belt due to the track tension and the position of track rollers located on a straight line. As the results, the track tension should be controlled to be as large as possible to increase the effective tractive effort and the traffic efficiency of power by means of some track tension sensor or rut depth sensor.

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